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**LAMB WAVE PROPAGATION IN A RESTRICTED  
GEOMETRY COMPOSITE PI-JOINT SPECIMEN  
(PREPRINT)**

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# LAMB WAVE PROPAGATION IN A RESTRICTED GEOMETRY COMPOSITE PI-JOINT SPECIMEN

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**ABSTRACT.** The propagation of elastic waves in a material can involve a number of complex physical phenomena, resulting in both subtle and dramatic effects on detected signal content. In recent years, the use of advanced methods for characterizing and imaging elastic wave propagation and scattering processes has increased, where for example the use of scanning laser vibrometry and advanced computational models have been used very effectively to identify propagating modes, scattering phenomena, and damage feature interactions. In the present effort, the propagation of Lamb waves within a narrow, constrained geometry composite pi-joint structure are studied using 3D finite element models and scanning laser vibrometry measurements, where the effects of varying sample thickness, complex joint curvatures, and restricted structure geometries are highlighted, and a direct comparison of computational and experimental results are provided for simulated and realistic geometry composite pi-joint samples.

**Keywords:** Composite Joint, Lamb Waves, Scanning Laser Vibrometry, Finite Element Modeling

**PACS:** 43.35.Pt; 81.70.-q; 43.35.Bf

## INTRODUCTION

In recent years, the use of composite materials in aircraft structures has increased, where for example the newly developed Boeing B787 and Airbus A350-XWB aircraft are expected to contain nearly 50% composite materials [1]. With increased composite material use, the need for structural integrity and damage assessment in these important materials has also increased, where ultrasonic sensing using guided Lamb waves has drawn considerable interest [2-4]. As pointed out by Giurgiutiu [5], the appeal of guided Lamb waves involves its capability for accomplishing measurements over extended regions with a minimal number of sensors. Combined with the availability of inexpensive piezoelectric sensor disks, the efficient generation and use of guided Lamb waves for damage detection, location, and quantification in thin-walled plates and shells is showing continued promise for use many practical applications.

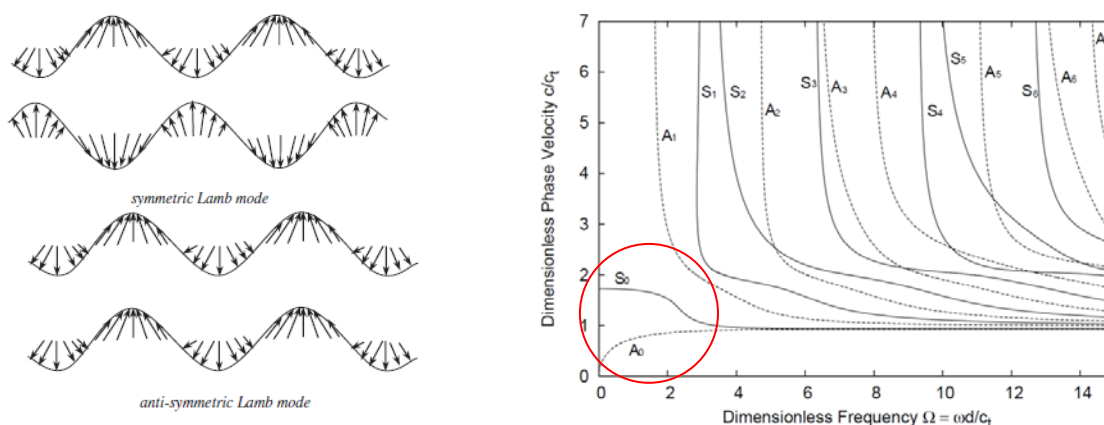
The use of guided Lamb waves has been studied extensively, with an increasing emphasis on the detection of damage in composite laminate materials [6-9]. In much of the work done to date, however, guided wave sensing has focused on large, open, plate-like structures typically found in wings and fuselage structures [10]. Although these structures are of concern for aerospace applications, structural joints are historically of critical importance for aircraft structural integrity assessments [11]. An increasing need exists, therefore, for sensing technologies capable of characterizing complex geometry and localized joints in composite structures.

In this paper, the characterization of a restricted geometry composite joint is studied using Lamb waves generated by bonded piezo sensor disks. The sensors were strategically placed on either side of the composite joint, which included a varying thickness, multi-layer composite structure with a vertical riser. Finite element models and scanning laser vibrometry measurements were used to study the generation and propagation of Lamb waves in the material, where both undamaged and damaged specimens are considered. Extensive use of forward models were used to understand Lamb wave interactions with the structure, where scanning laser vibrometry measurements were used as a method for model validation. The remainder of the manuscript includes a brief technical background on Lamb wave sensing in a restricted geometry composite joint, followed by a description of the forward models, experimental studies, results, and conclusions.

## LAMB WAVE PROPAGATION IN A RESTRICTED GEOMETRY PI-JOINT

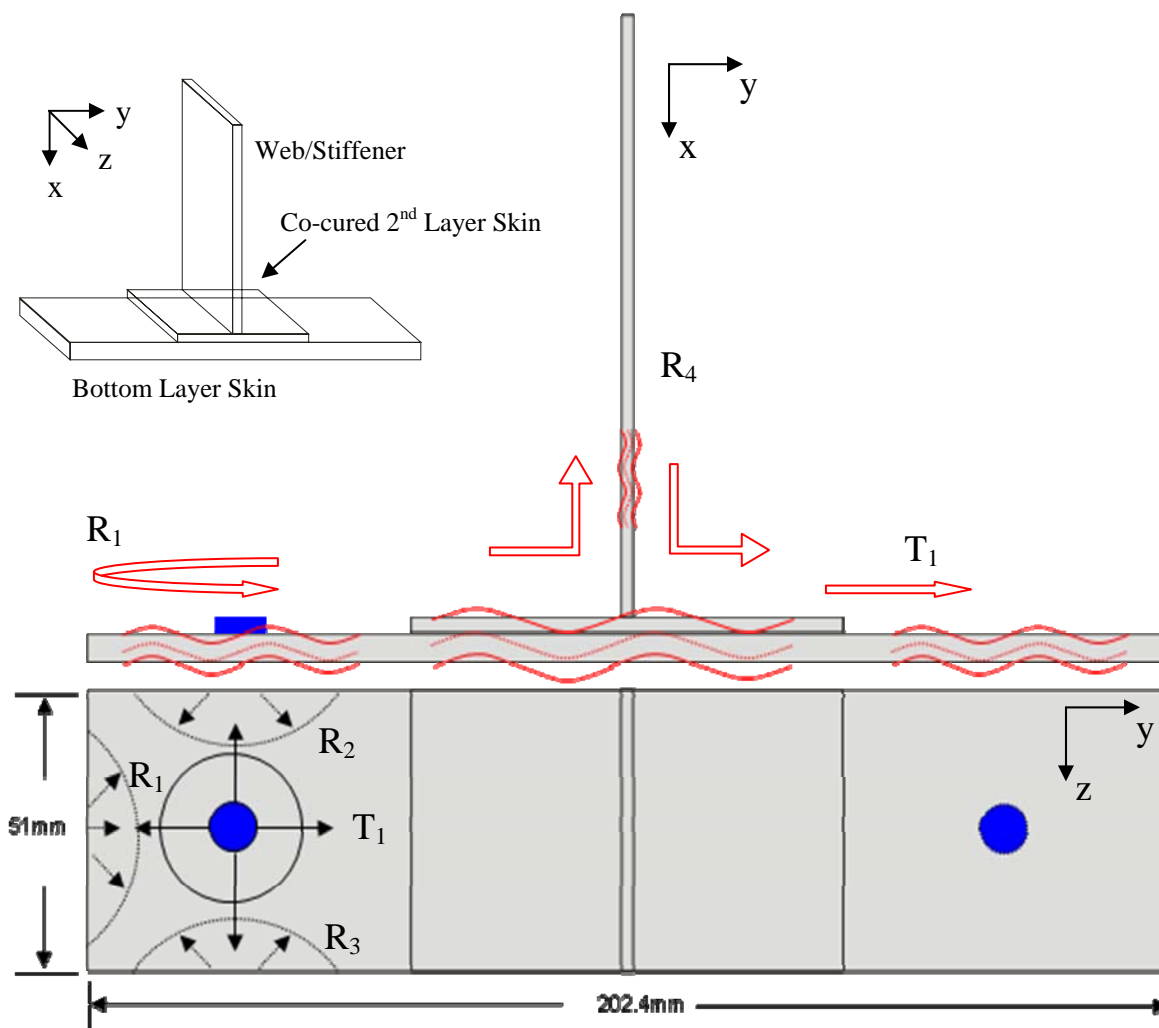
### Physics of Wave Propagation Problem

Guided Lamb waves involve the propagation of elastic waves in a bounded medium whose particle motion lies in the plane defined by the plate normal to the direction of wave propagation [12]. In contrast to bulk waves, guided Lamb waves involve two infinite sets of propagating modes, referred to as symmetric  $S_n$  and antisymmetric  $A_n$  modes. In most instances, the  $S_n$  and  $A_n$  modes are dispersive in nature, where the velocity of a propagating mode,  $c_n$ , depends on the ultrasonic frequency, the elastic constants and density of the material, and the ratio of the plate thickness,  $d$ , and propagating mode wavelength,  $\lambda$ , which determine the effective stiffness of the plate [2,3,12]. For a given thickness  $d$  and frequency  $f$ , the characteristic propagating modes and wave velocities can be established using dispersion curves calculated from the Rayleigh–Lamb relations [2,3,12].



**FIGURE 1.** Schematic diagram of symmetric and antisymmetric guided Lamb wave modes (left), and example of dispersion curve for propagating modes in a thin-walled, plate structure (right).

It is widely known that the phenomenon of velocity dispersion can lead to significant complexity with respect to experimentally observed Lamb wave signals. As a result, the use of single mode, or ‘tuned’, excitation methods have been developed, where a single fundamental mode is preferentially excited and other modes are suppressed. As originally described by Giurgiutiu [5], the direct shear-layer coupling between an adhesively bonded piezoelectric sensor disk and a structure can lead to an inherent and preferred coupling of energy into a particular Lamb wave mode by frequency tuning. This represents a key feature for minimizing signal complexity in a practical Lamb wave measurement process when geometric/material complexity exists (Figure 2). The fundamental  $A_0$  mode, for example, can effectively be isolated for generation and detection purposes, where previous research has shown signal content simplification and enhanced interactions of  $A_0$  energy with delaminations in composite laminates [5].



**FIGURE 2.** Schematic diagram of thin 2-layer, restricted-geometry joint with a vertical web attachment. A schematic representation of the piezo disk sensor placement and propagating guided waves are also depicted where guided Lamb waves propagate in the thickness of the sample in the X-Y plane (top schematic view), and omnidirectional waves propagate away from the sensor in the Y-Z plane (bottom schematic view).

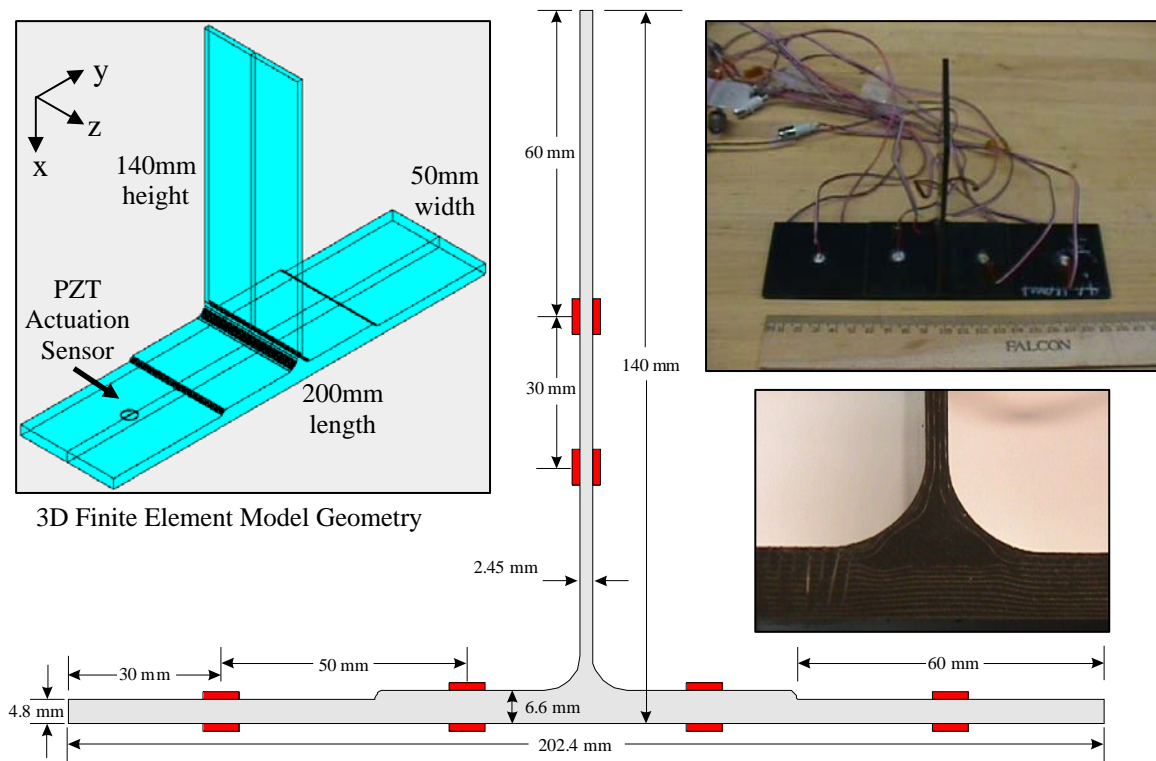
With regard to wave propagation in the restricted geometry sample depicted in Figure 2, several important points can be made. For low-frequency waves of  $f = 100\text{kHz}$ , the propagating modes are restricted to the two lowest modes  $A_0$  and  $S_0$  depicted in the dispersion curve diagram of Figure 1. In addition, mode selection can be used to

preferentially excite  $A_0$  versus  $S_0$  [5,13], where a single  $A_0$  mode exists within the material volume. For the composite material used in the current study (a carbon fiber reinforced polymer, CFRP), wavelengths and phase velocities for the  $A_0$  mode were near 10 mm and 1500 m/s, respectively. Due to the restricted sample geometry, reflective waves are quickly generated at the left end ( $R_1$ ) and top-bottom sidewalls ( $R_2$  and  $R_3$ ) of the sample in the axial-transverse plane (Y-Z). These reflected waves propagate and superposition within the 3D volume in a semi-coherent nature, resulting in signal content trailing behind the direct-transmit wave ( $T_1$ ) with 25-100 microsecond time delays for detection positions along the sample length. The variation and increase of thickness in the co-cured joint region can also cause shifts in the frequency-thickness product (see Figure 1), with corresponding changes in the phase velocity,  $c_p$ , and wavelength,  $\lambda$ , of the propagating modes in those regions. Propagation and re-direction of energy into the vertical web region can also occur (Figure 2), with mode conversion and additional dispersive characteristics at the various reflective surfaces ( $R_4$ ) and thickness variation positions.

### **Numerical Modeling Approach and Studies**

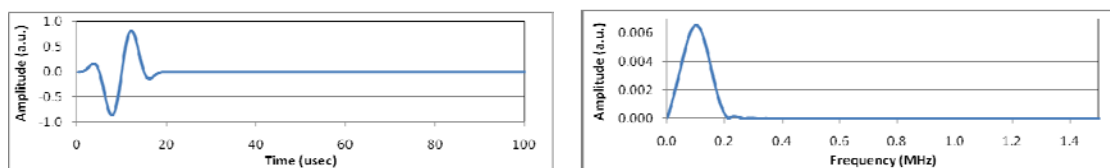
A series of 3D-finite element models were used to study the behavior of the Lamb wave interactions within the composite joint depicted in Figure 3. The model was developed in a commercially available finite element package PZFlex, which is designed and optimized for elastic wave propagation analysis. The model geometry depicted in Figure 3 was chosen to match as closely as possible the cross-sectional profile and 3D characteristics of a composite joint sample used in mechanical testing studies. Figure 3 provides a schematic cross-sectional diagram of the composite joint test article, and digital images of a sample showing bonded piezo sensors and composite layers in cross-section. The sample included a 40-ply, quasi-isotropic lay-up [0/90/45/-45]5S for the graphite fiber/epoxy composite skin (Newport Adhesives and Composites, NCT-350-GT145-TR50S), which was co-cured with a 20-ply vertical riser/web lay-up [0/45/90/-45/-45/45/45/90]S, where  $\frac{1}{2}$  of the web plies were split and re-directed 90-degrees into the top surface of the skin during the curing process [14]. The overall length, width, and thickness of the skin region were 202.4 mm, 51 mm, and 4.8 mm, respectively. In the overlap region of the skin, the thickness increases to 6.6 mm due the additional 2 composite plies, while the thickness of the vertical riser/web region was 2.45 mm with an overall height of 140 mm. The thickened region extends out ~42.8 mm on either side of the vertical riser/web region along the length of the sample. As shown in the inset images and schematic diagram in Figure 3, piezoelectric sensors (APC D-6.35mm-0.2mm-850WFB) were bonded on the top and bottom surfaces of the composite skin, with four additional sensors placed symmetrically on either side of the web. The sensors were bonded to the specimen using M-Bond adhesive, and were located along the length and height of the specimen as depicted in Figure 3. The sensors were 6.35 mm round disks of PZT, with a thickness of 200 microns, and were polarized to produce a radial shearing force when actuated.

The 3D finite element model used to approximate the realistic sample geometry included a 200 mm long x 50 mm wide x 140 mm high structure (see upper right inset graphic in Figure 3). A single piezoelectric sensor (PZT:fpz29) was used to generate Lamb waves in the model and was located on the top left surface of the skin as depicted in Figure 3. The sensor had a diameter of 6.35 mm and a thickness of 250 microns. A hard epoxy bonding layer 250 microns thick was used in the model to couple energy into the composite. The model had a grid element spacing of 250 microns, which resulted in  $560 \times 800 \times 100 = 44,800,000$  elements. A symmetry plane was located at the midpoint of the sample in the transverse direction (z-plane) extending along the sample geometry length.



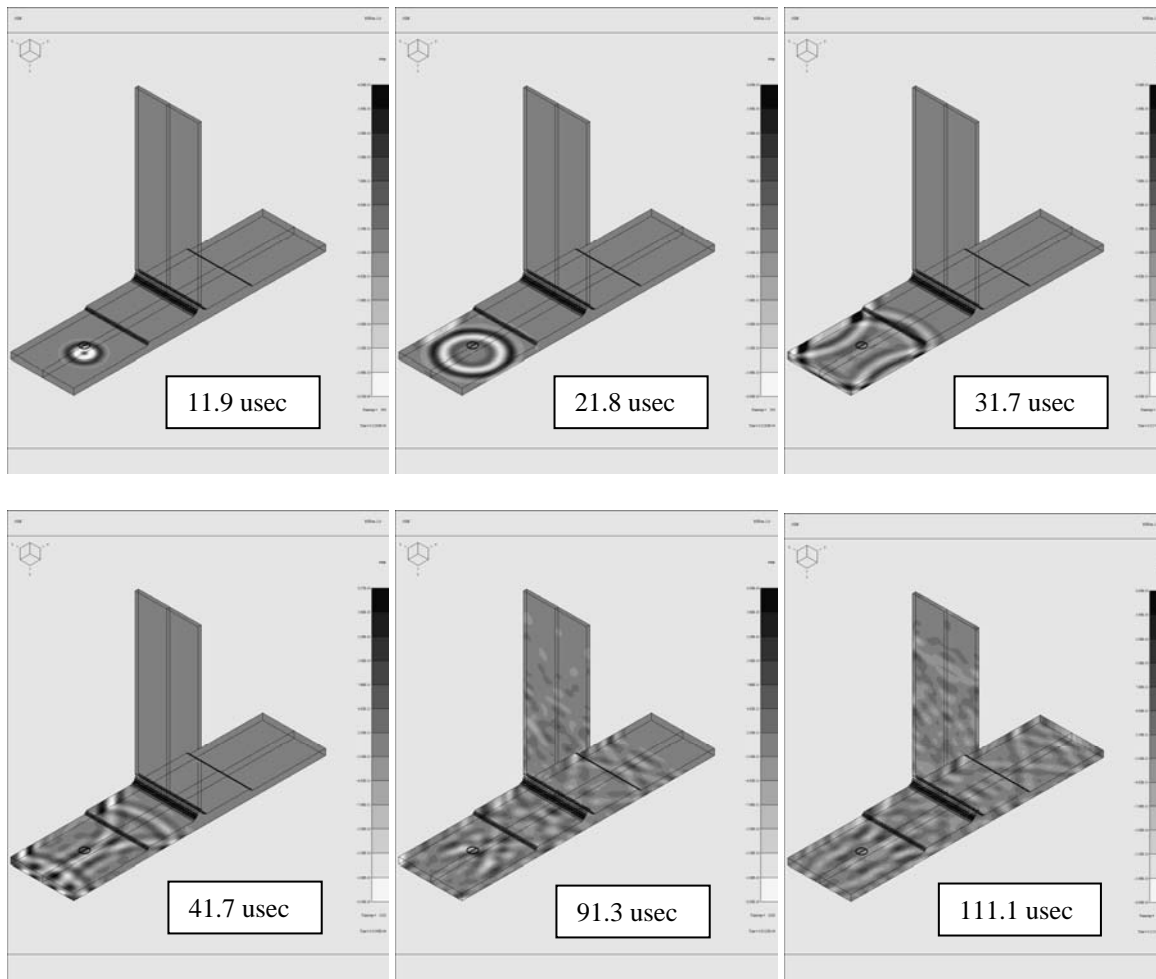
**FIGURE 3.** Schematic of 3D finite element model geometry (upper left), cross-sectional details (center), and digital images of specimen (right).

The material properties of the composite were treated as being isotropic and homogeneous in the current model with a density of  $1500 \text{ kg/m}^3$ , a longitudinal velocity of  $3946 \text{ m/s}$ , and a shear velocity of  $1941 \text{ m/s}$ . Free-boundary conditions were applied to all of the exposed surfaces of the model. The excitation pulse and FFT spectrum for the  $100 \text{ kHz}$  excitation used in the model are depicted in Figure 4, respectively. Discretization of the domain was set to 60 elements per wavelength, which provided adequate stability and convergence of the model, and an accurate representation of the Lamb wave propagation and scattering features. Model run times were typically  $200 \text{ usec}$  with a  $\text{Dt} = 0.0397 \text{ usec}$ .

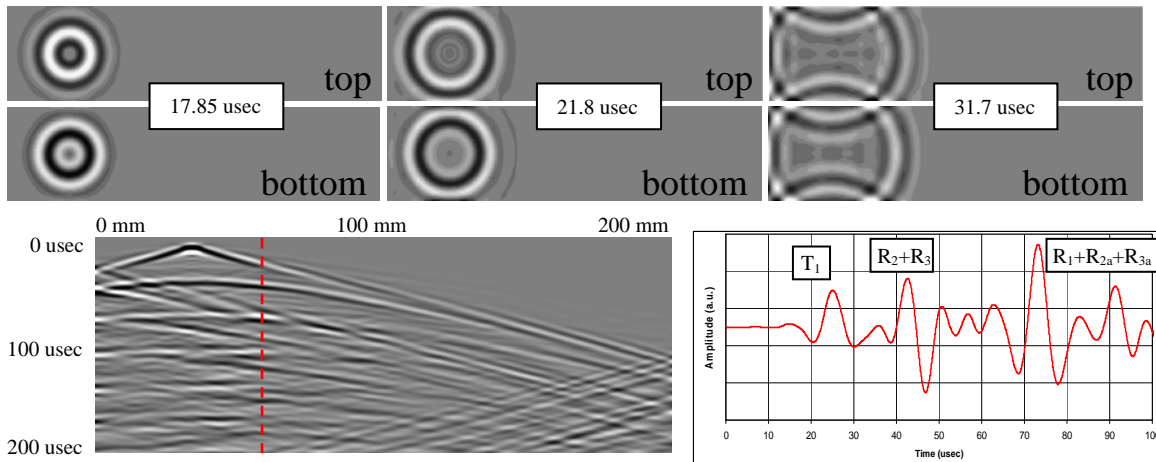


**FIGURE 4.** Finite element model  $100 \text{ kHz}$  excitation signal (left), and its frequency spectrum (right).

Figures 5 and 6 depict model results for the composite joint studies. Figure 5 depicts x-displacement component amplitude levels for different time steps between  $11.9 \text{ usec}$  and  $111.1 \text{ usec}$ , where circularly symmetric wave can be seen propagating away from the piezoelectric actuator location with reflections from the sides and left end of the sample occurring at  $20 \text{ usec}$  and  $30 \text{ usec}$ , respectively. Figure 6 depicts x-displacement amplitude levels occurring on the top and bottom surfaces of the sample, where anti-symmetric motions occur between the two surfaces, consistent with  $A_0$  mode propagation. Figure 6 also depicts a B-scan image (left bottom) and a detected signal (right bottom) for the  $y, z = (60\text{mm}, 25\text{mm})$  position, where an  $A_0$  phase velocity of  $1485 \text{ m/s}$  was estimated. Reflected wave features due to the restricted geometry are observed in both cases for  $R_1$ ,  $R_2$ , and  $R_3$ .



**FIGURE 5.** Model-based x-displacement amplitudes for 3D composite joint at increasing times.



**FIGURE 6.** X-displacement model results: top/bottom skin surface images (top), B-scan for centerline of bottom surface (bottom left), and detected signal at  $y, z = (60\text{mm}, 25\text{mm})$  on bottom surface (bottom right).

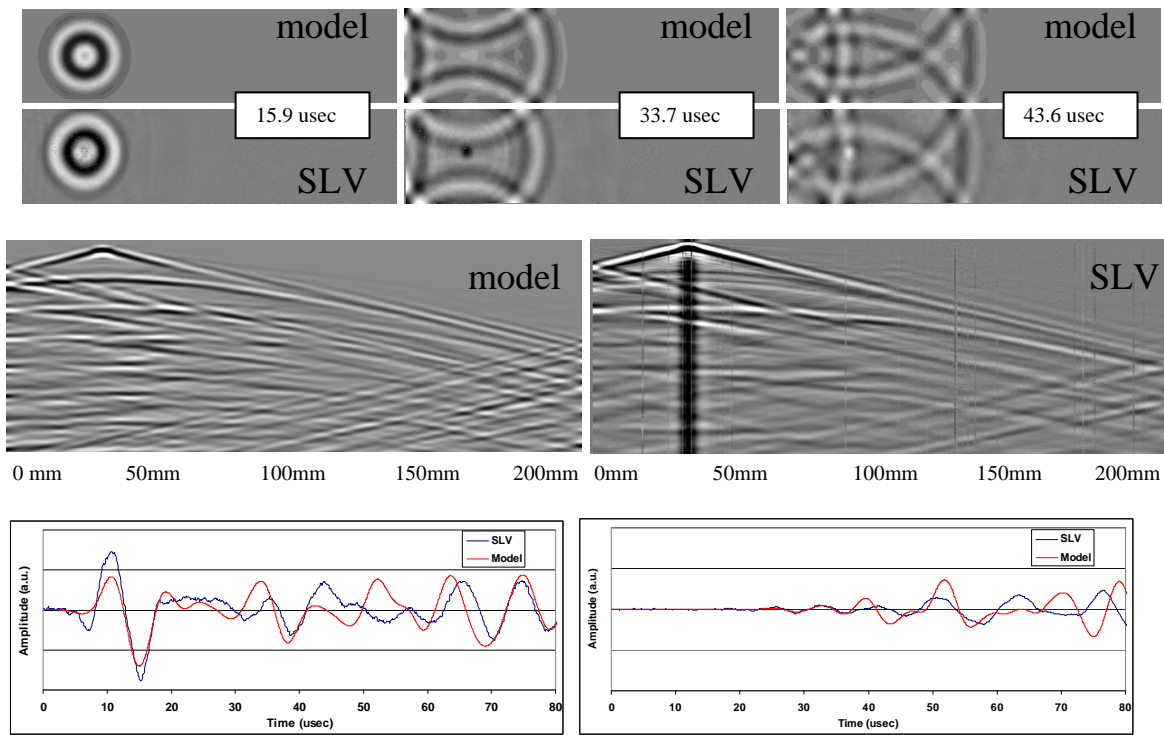
### **Model Validation using Scanning Laser Vibrometry**

In recent years, the use of advanced methods for characterizing and imaging elastic wave propagation and scattering processes has increased, where for example the use of scanning laser vibrometry (SLV) has been used very effectively to identify propagating



modes, scattering phenomena, and damage feature properties [15,16]. A typical scanning laser vibrometry system provides a means for measuring the local velocity or displacement levels on a material surface with spatial resolutions approaching 1 micron. In the present effort, a scanning laser vibrometry system was used as a validation tool for the finite element modeling results presented in the previous section.

Figure 7 provides a comparison of model generated and scanning laser vibrometry measurement results for the bottom surface of the 3D composite joint specimen. A single bonded piezoelectric sensor disk was used to generate Lamb waves in the sample for the SLV measurements at the same location on the top skin used in the model studies (see Figure 3). Three examples of the ultrasonic displacement field are shown in Figure 7 (top sets of images) for the x-displacement on the bottom surface of the composite skin. Good agreement is observed between the propagation speeds and wave characteristics in all three cases. A comparison of B-scans extracted for the x-displacement along the centerline of the bottom surface of the composite skin is presented in Figure 7 (center set of images). Reasonable agreement between the model and experimental measurements is again observed. Estimations of the  $A_0$  phase velocity were made using the B-scan results and were 1485 m/s and 1462 m/s for the model and scanning laser vibrometry signals, respectively. A comparison of x-displacement signals at  $y,z = (0\text{mm}, 25\text{mm})$  and  $(100\text{mm}, 25\text{mm})$  are shown in the bottom left and right plots in Figure 7, respectively, where good qualitative agreement is seen in the results.



**FIGURE 7.** Comparison of finite element model and scanning laser vibrometry results; x-displacement images (top), B-scans for centerline of bottom surfaces (center), and signals at 50 mm and 100mm (bottom).

## CONCLUSIONS

The present research utilized finite element analysis models to study Lamb wave propagation and scattering in a restricted geometry composite structural joint. Selective mode tuning with a 100 kHz pulse generated the lowest order antisymmetric  $A_0$  mode in the structure, which was verified by comparing model-generated displacement fields on

the top and bottom surfaces of the composite skin. Due to the restricted geometry conditions, which included a 50 mm wide by 200 mm long composite structure, significant reflections occurred in the sample, which were semi-coherent in nature and were distinguishable in the modeling results through B-scan and displacement signal analysis. Validation of model predictions was accomplished using scanning laser vibrometry measurements, where excellent agreement was seen for model versus experimental results for displacement field images, B-scan analyses, and displacement signal content.

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